

# Economics of Nonrenewable Resources

## Lecture 4

### 1. Nonrenewable Resources

- Minerals
  - Coal, Oil, Tungsten, Nickel etc.
  - Fixed stock
  - Not renewable (fish, trees, etc.)
- Efficient use over time
  - Rate of extraction

- Scarcity
  - Geologic and Economic dimensions of scarcity
    - Geologic is physical side
    - Economics recognizes that “availability” depends on extraction cost and willingness to pay (technology change and resource prices)
      - Tar sands in Canada for oil
  - McKelvey diagram

Cumulative Production	IDENTIFIED RESOURCES			UNDISCOVERED RESOURCES	
	Demonstrated		Inferred	Probability Range	
	Measured	Indicated		Hypothetical	(or) Speculative
ECONOMIC	Reserves		Inferred Reserves		
MARGINALLY ECONOMIC	Marginal Reserves		Inferred Marginal Reserves		+
SUB-ECONOMIC	Demonstrated Subeconomic Resources		Inferred Subeconomic Resources		+

Other Occurrences	Includes nonconventional and low-grade materials
-------------------	--

- Be wary of Physical indicator of scarcity
  - Reserves-to-Use Ratio
  - Historically have been wrong
    - Ignore technology, prices, substitutes
- Many Armageddons
  - Jevons “The Coal Question”
  - Reverend Malthus
  - Simon vs. Ehrlich (read Tierney NYT 1990)

- Efficient Extraction in 2 Periods
  - Assume: fixed quantity (20 barrels)
  - Assume: 2 periods → today and tomorrow
  - Assume: stable preferences and cost functions
  - Ask: What is the efficient rate of extraction?
  - Show: Market should account for future use of resource and does through concept of “User Cost” or “Scarcity Rent”

- Consider myopic result (ignoring next period)

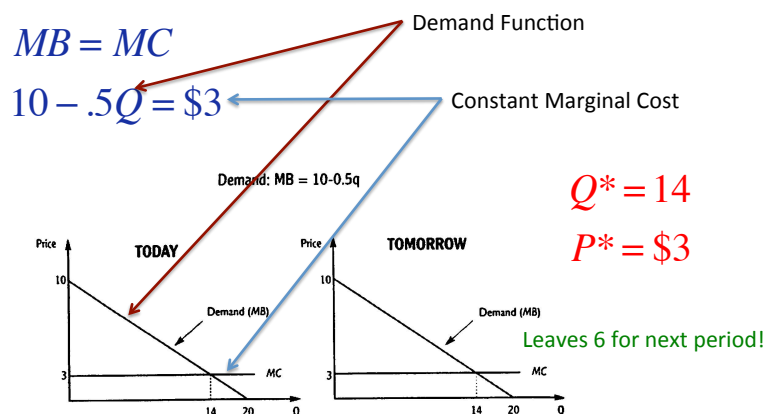


Figure 6.2 The problem with (myopic) static efficiency in the case of a scarce resource. Static efficiency would imply extracting fourteen barrels in each period—more than the total stock of twenty barrels.

Static efficiency ignores effect of loss economic value in next period!

- Consider dynamic result
  - Account for impact of current use on future lost
  - Using today implies loss use tomorrow
  - There is a second real piece to marginal cost → user cost or scarcity rent
  - Dynamic result maximizes value over the sum of two periods → today and tomorrow

- Efficient dynamic conditions
  - Set net values equal over the two time periods
  - Why is this?

$$PV(MB_1 - MC_1) = PV(MB_2 - MC_2)$$

$$10 - .5Q_1 - 3 = \frac{10 - .5Q_2 - 3}{1 + .10}$$

$$Q_1^* = 10.19$$

$$Q_2^* = 20 - Q_1^* = 9.81$$

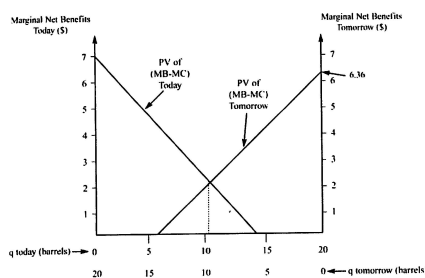


Figure 6.3 Nonrenewable resource extraction: the two-period model.

- Rearranging equation ....

$$MB_1 - MC_1 - \delta(MB_2 - MC_2) = 0$$

Marginal Benefit  
Of Current Use

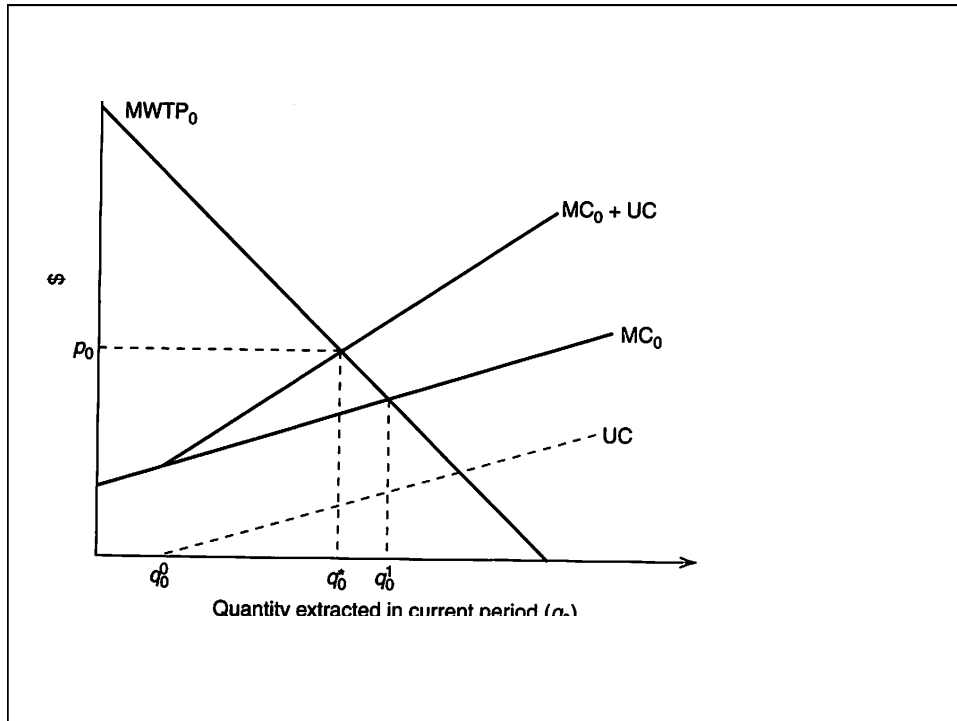
Marginal Cost  
Of Current Use

Discount rate

Marginal Value of  
Of Future Use  
- Oil left in the ground for tomorrow

Marginal user cost is  
a great indicator of scarcity.

-Scarcity Rent  
-User Cost  
Almost like an external cost on  
current consumption



- General Model

$$\left\{ \text{Max} \sum_{t=0}^T \rho^t U(q_t) \mid \text{st} \ R_0 - \sum_{t=0}^T q_t = 0 \right\}$$

$$L = \text{Max} \sum_{t=0}^T \rho^t U(q_t) + \mu \left\{ R_0 - \sum_{t=0}^T q_t \right\}$$

$$U'(q_0) = \rho U'(q_1) = \rho^2 U'(q_2) = \dots = \rho^T U'(q_T)$$

→ Marginal Utility of extraction must grow at the rate of discount .... And Hotelling Rule applies.

- The Hotelling Rule

- Nonrenewable resource stocks should increase in value at a rate equal to that of other types of assets in the market (i.e., something like the market rate of interest)
- Leaving oil (or whatever mineral) in the ground is an investment with some return (rent)
  - If they grow at a slower rate → extract
  - If they grow at a faster rate → wait

- Hotelling Rule and Profit Maximizing Firm

$$\begin{aligned} \frac{MUC_2 - MUC_1}{MUC_1} &= \frac{(P_2 - MC_2) - (P_1 - MC_1)}{P_1 - MC_1} \\ &= \frac{(5.095 - 3) - (4.905 - 3)}{4.905 - 3} \\ &= .10 \end{aligned}$$

- Comments
  - Price and Quantity paths
  - Making the model more sophisticated:
    - Technological Change (future cost curves shift in)
    - Increasing cost over time due to depletion (future cost curves shift out)
    - Increasing population and demand
    - Uncertainty
    - Backstop technologies
  - Read Livernois

- Market Failure
  - Externalities in mining and other down stream operations
  - Resource will incomplete assignment of property rights (open access resources) → expect race to pump
    - Groundwater Aquifer
    - Some Oil Wells